

# Mathematics (MATH)

The department offers a major in Mathematics, a major in Mathematics with a Concentration in Applied Mathematics, a major in Mathematics with a Concentration in Pure Mathematics, and a minor in Mathematics. Students completing the major in Mathematics may qualify for the BA degree or the BS degree, depending upon how they meet the college's general education requirement in the natural sciences. The department prepares students for mathematics related careers, including teacher education, and for graduate studies in mathematics.

Students majoring in Mathematics may obtain an Emphasis in Computational Science (<http://catalog.wofford.edu/archive/2017-2018/courses-programs-departments/computer-science/#emphasisrequirements>). The interdisciplinary field of computational science applies computer science and mathematics to the sciences.

Students in the Teacher Education Program who are seeking to complete secondary education licensure requirements to teach mathematics should refer to the *Teacher Education Handbook* and consult with the chairs of the Departments of Mathematics and Education to develop a curricular plan that will meet the requirements for both fields of study.

## Honors Courses and In-Course Honors

The Department of Mathematics encourages its students to undertake honors work. For further information, the student is referred to the sections on Honors Courses (<http://catalog.wofford.edu/archive/2017-2018/academics/academic-honors/honors-courses>) and In-Course Honors (<http://catalog.wofford.edu/archive/2017-2018/academics/academic-honors/honors-courses>) in the *Catalog*.

## Chair

Joseph A. Spivey

## Professors

Matthew E. Cathey

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## Requirements for the Major in Mathematics

### Corequisite

COSC 235	Programming & Problem Solving	
<b>Core Requirements</b>		<b>15</b>
MATH 181	Calculus I	
MATH 182	Calculus II	
MATH 210	Multivariable Calculus	
MATH 220	Linear Algebra	
MATH 260	Introduction to Mathematical Proof	
<b>Electives</b>		<b>18</b>
Select six Math courses at the 200-level or higher, at least three of which must be at the 400-level.		
<b>Total Hours</b>		<b>33</b>

## Requirements for the Major in Mathematics with a Concentration in Applied Mathematics <sup>1</sup>

### Corequisite

COSC 235	Programming & Problem Solving	
<b>Core Requirements</b>		<b>21</b>
MATH 181	Calculus I	
MATH 182	Calculus II	
MATH 201	Modeling & Simulation	
or MATH 320	Mathematical Modeling	
MATH 210	Multivariable Calculus	
MATH 220	Linear Algebra	
MATH 240	Differential Equations	
MATH 260	Introduction to Mathematical Proof	
<b>Upper Level Electives</b>		<b>9</b>
Select three courses from the following (or other 400-level courses as approved by the Coordinator of Applied Math):		
MATH 330	Numerical Methods	
MATH 421	Probability and Statistics I	
MATH 422	Probability and Statistics II	
MATH 424	Advanced Game Theory	
MATH 431	Abstract Algebra I	
MATH 435	Cryptology	
MATH 441	Mathematical Analysis I	
MATH 445	Nonlinear Dynamics and Chaos Theory	
MATH 446	Partial Differential Equations	
<b>Electives</b>		<b>6</b>
Select two Math courses at the 200-level or higher.		
<b>Research (0-3 credit hours)</b>		
Each student must complete a summer research project, a semester of independent research, or an honors course. This requires the prior approval of the Applied Math Coordinator.		
<b>Area of Application (6-12 credit hours)</b>		
Each student must choose an area of application (Accounting, Finance, Biology, Chemistry, Computer Science, Economics, Environmental Studies, Philosophy, Physics or Psychology) and complete two or three courses as approved by the Applied Math Coordinator.		
<b>Total Hours</b>		<b>36</b>

<sup>1</sup> The total number of credit hours for the Major with the Applied Math Concentration is 36-39 depending on the the number of research hours earned; this does NOT include the hours associated with the Co-requisite or the Area of Application.

## Requirements for the Major in Mathematics with a Concentration in Pure Mathematics <sup>2</sup>

### Corequisite

COSC 235	Programming & Problem Solving	
<b>Core Requirements</b>		<b>15</b>
MATH 181	Calculus I	
MATH 182	Calculus II	

MATH 210	Multivariable Calculus
MATH 220	Linear Algebra
MATH 260	Introduction to Mathematical Proof

**Upper-Level Requirements** 9

Select three courses from the following:

MATH 431	Abstract Algebra I
MATH 432	Abstract Algebra II
MATH 441	Mathematical Analysis I
MATH 442	Mathematical Analysis II

**Upper-Level Electives** 3

Select one course from the following (or other course at the 400-level as approved by the Coordinator of Pure Math):

MATH 410	Geometry
MATH 415	Topology
MATH 432	Abstract Algebra II
MATH 439	Elementary Number Theory
MATH 442	Mathematical Analysis II
MATH 448	Functions of a Complex Variable

**Applied Math Electives** 6

Select two Applied Math courses from the following (or other courses as approved by the Coordinator of Pure Math):

MATH 201	Modeling & Simulation
MATH 212	Vector Calculus
MATH 235	Discrete Mathematical Models
MATH 240	Differential Equations
MATH 320	Mathematical Modeling
MATH 330	Numerical Methods
MATH 421	Probability and Statistics I
MATH 422	Probability and Statistics II
MATH 435	Cryptography
MATH 442	Mathematical Analysis II
MATH 446	Partial Differential Equations
MATH 448	Functions of a Complex Variable

**Pure Math Elective** 3

Select one Pure Math course from the following (or other course as approved by the Coordinator of Pure Math):

MATH 310	History of Mathematics
MATH 410	Geometry
MATH 415	Topology
MATH 432	Abstract Algebra II
MATH 439	Elementary Number Theory
MATH 442	Mathematical Analysis II
MATH 448	Functions of a Complex Variable

**Research**

Each student must complete a summer research project, a semester of independent research, or an honors course. This requires the prior approval of the Pure Math Coordinator.

Total Hours 36

<sup>2</sup> The total number of credit hours for the Major with the Pure Math Concentration is 36-39 depending on the number of research hours earned; this does NOT include the hours associated with the Co-requisite.

## Requirements for the Mathematics Major and Program in Teacher Education

Students in the Teacher Education Program who are seeking to complete licensure requirements to teach mathematics at the secondary level should refer to the *Teacher Education Handbook* and consult with the chairs of the Departments of Mathematics and Education to develop a plan for meeting all requirements.

**Corequisite**

COSC 235	Programming & Problem Solving
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**Core Requirements** 27

MATH 140	Statistics
MATH 181	Calculus I
MATH 182	Calculus II
MATH 220	Linear Algebra
MATH 235	Discrete Mathematical Models
MATH 260	Introduction to Mathematical Proof
MATH 310	History of Mathematics
MATH 410	Geometry
MATH 431	Abstract Algebra I

**Electives** 6

Select one course from the following:

MATH 210	Multivariable Calculus
MATH 240	Differential Equations
MATH 320	Mathematical Modeling

Select one additional Math course at the 200-level or higher

Total Hours 33

## Requirements for the Minor in Mathematics

MATH 181	Calculus I	3
MATH 182	Calculus II	3
Select four additional Math courses at the 200-level or higher		12
Total Hours		18

**MATH 120. Appreciation of Mathematics. 3 Hours.**

An exploration of topics which illustrate the power and beauty of mathematics, with a focus on the role mathematics has played in the development of Western culture. This course is designed for students who are not required to take statistics or calculus as part of their studies. Students who previously earned credit for a math course at the 200-level or higher are not permitted to enroll or earn credit for this course.

**MATH 140. Statistics. 3 Hours.**

An introduction to statistical thinking and the analysis of data using such methods as graphical descriptions, correlation and regression, estimation, hypothesis testing, and statistical models.

**MATH 160. Calculus for the Social Sciences. 3 Hours.**

A graphical, numerical and symbolic introduction to the theory and applications of derivatives and integrals of algebraic, exponential, and logarithmic functions, with an emphasis on applications in the social sciences.

**MATH 181. Calculus I. 3 Hours.**

A graphical, numerical, and symbolic study of the theory and applications of the derivative of algebraic, trigonometric, exponential, and logarithmic functions, and an introduction to the theory and applications of the integral. Suitable for students of both the natural and the social sciences.

**MATH 182. Calculus II. 3 Hours.**

A graphical, numerical, and symbolic study of the theory, techniques, and applications of integration, and an introduction to infinite series and/or differential equations.

**Prerequisite:** MATH 181 with a minimum grade of D.

**MATH 201. Modeling & Simulation. 3 Hours.**

A course in scientific programming, part of the inter-disciplinary field of computational science. Large, open-ended, scientific problems often require the algorithms and techniques of discrete and continuous computational modeling and Monte Carlo simulation. Students learn fundamental concepts and implementation of algorithms in various scientific programming environments. Throughout, applications in the sciences are emphasized. Cross-listed as Computer Science 201.

**Prerequisite:** MATH 181 with a minimum grade of D.

**MATH 210. Multivariable Calculus. 3 Hours.**

A study of the geometry of three-dimensional space and the calculus of functions of several variables.

**Prerequisite:** MATH 182 with a minimum grade of D.

**MATH 212. Vector Calculus. 3 Hours.**

A study of vectors and the calculus of vector fields, highlighting applications relevant to engineering such as fluid dynamics and electrostatics.

**Prerequisite:** MATH 182 with a minimum grade of D.

**MATH 220. Linear Algebra. 3 Hours.**

The theoretical and numerical aspects of finite dimensional vector spaces, linear transformations, and matrices, with applications to such problems as systems of linear equations, difference and differential equations, and linear regression.

**Prerequisite:** MATH 182 with a minimum grade of D.

**MATH 235. Discrete Mathematical Models. 3 Hours.**

An introduction to some of the important models, techniques, and modes of reasoning of non-calculus mathematics. Emphasis on graph theory and combinatorics. Applications to computing, statistics, operations research, and the physical and behavioral sciences.

**Prerequisite:** MATH 182 with a minimum grade of D.

**MATH 240. Differential Equations. 3 Hours.**

The theory and application of first- and second-order differential equations including both analytical and numerical techniques.

**Prerequisite:** MATH 182 with a minimum grade of D.

**MATH 250. Introduction to Technical Writing. 1 Hour.**

An introduction to technical writing in mathematics and the sciences with the markup language LaTeX, which is used to typeset mathematical and scientific papers, especially those with significant symbolic content.

**MATH 260. Introduction to Mathematical Proof. 3 Hours.**

An introduction to rigorous mathematical argument with an emphasis on the writing of clear, concise mathematical proofs. Topics will include logic, sets, relations, functions, and mathematical induction. Additional topics may be chosen by the instructor.

**Prerequisite:** MATH 182 with a minimum grade of D.

**MATH 270. Independent Study in Mathematics. 1 to 3 Hours.**

Independent study of selected topics in Mathematics at an intermediate level. Specific topics vary from semester to semester. Permission of the instructor required.

**MATH 280. Selected Topics in Mathematics. 1 to 4 Hours.**

Selected topics in mathematics at the introductory or intermediate level.

**MATH 310. History of Mathematics. 3 Hours.**

A survey of the history and development of mathematics from antiquity to the twentieth century.

**Prerequisite:** MATH 260 with a minimum grade of D.

**MATH 320. Mathematical Modeling. 3 Hours.**

The study of problem-solving strategies to solve open-ended, real-world problems.

**Prerequisite:** MATH 210 with a minimum grade of D or MATH 220 with a minimum grade of D or MATH 240 with a minimum grade of D.

**MATH 330. Numerical Methods. 3 Hours.**

A study of the theory and computer implementation of numerical methods. Topics include error analysis, zeros of polynomials, numerical differentiation and integration, and systems of linear equations.

**Prerequisite:** MATH 220 with a minimum grade of D.

**MATH 410. Geometry. 3 Hours.**

A study of the foundations of Euclidean geometry with emphasis on the role of the parallel postulate. An introduction to non-Euclidean (hyperbolic) geometry and its intellectual implications.

**Prerequisite:** MATH 260 with a minimum grade of D.

**MATH 415. Topology. 3 Hours.**

An introduction to topological spaces. Topics will include examples of topological spaces, standard constructions of topological spaces, continuous maps, topological properties, homotopies, homeomorphisms, and simplicial complexes.

**Prerequisite:** MATH 260 with a minimum grade of D.

**MATH 421. Probability and Statistics I. 3 Hours.**

A study of probability models, random variables, estimation, hypothesis testing, and linear models, with applications to problems in the physical and social sciences.

**Prerequisite:** MATH 210 with a minimum grade of D and MATH 260 with a minimum grade of D.

**MATH 422. Probability and Statistics II. 3 Hours.**

A study of probability models, random variables, estimation, hypothesis testing, and linear models, with applications to problems in the physical and social sciences.

**Prerequisite:** MATH 421 with a minimum grade of D.

**MATH 424. Advanced Game Theory. 3 Hours.**

Game Theory is an analytical tool that models strategic interactions. It is widely used in economics, political science, biology, sociology, and psychology. This advanced class is intended to provide a more rigorous introduction to the main concepts and techniques of the field. These techniques will be used to investigate relevant social phenomena, such as evolutionary games, auction theory, the "prisoner's dilemma," the "tragedy of the commons," tacit collusion, competition among firms, and strategic interactions in labor, credit, and product markets. The most important classes of games will be analyzed (zero-sum games, cooperation problems, coordination games, bayesian games, signaling games, etc.), as well as the most important solution concepts (rationalizability, nash equilibrium in pure and mixed strategies, bayesian nash equilibrium, and evolutionarily stable strategies). This course will also introduce students to the main techniques of game-theoretic mathematical modelling.

**Prerequisite:** MATH 210 with a minimum grade of D.

**MATH 431. Abstract Algebra I. 3 Hours.**

The axiomatic development of abstract algebraic systems, including groups, rings, integral domains, fields, and vector spaces.

**Prerequisite:** MATH 220 with a minimum grade of D and MATH 260 with a minimum grade of D.

**MATH 432. Abstract Algebra II. 3 Hours.**

The axiomatic development of abstract algebraic systems, including groups, rings, integral domains, fields, and vector spaces.

**Prerequisite:** MATH 431 with a minimum grade of D.

**MATH 435. Cryptology. 3 Hours.**

An introduction to cryptology and modern applications. Students will study various historical and modern ciphers and implement select schemes using mathematical software. Cross-listed with COSC 435.

**Prerequisite:** MATH 220 with a minimum grade of D and (MATH 235 with a minimum grade of D or MATH 260 with a minimum grade of D).

**MATH 439. Elementary Number Theory. 3 Hours.**

A study of the oldest branch of mathematics, this course focuses on mathematical properties of the integers and prime numbers. Topics include divisibility, congruences, diophantine equations, arithmetic functions, primitive roots, and quadratic residues.

**Prerequisite:** MATH 260 with a minimum grade of D.

**MATH 441. Mathematical Analysis I. 3 Hours.**

A rigorous study of the fundamental concepts of analysis, including limits, continuity, the derivative, the Riemann integral, and sequences and series.

**Prerequisite:** MATH 210 with a minimum grade of D and MATH 260 with a minimum grade of D.

**MATH 442. Mathematical Analysis II. 3 Hours.**

A rigorous study of the fundamental concepts of analysis, including limits, continuity, the derivative, the Riemann integral, and sequences and series.

**Prerequisite:** MATH 441 with a minimum grade of D.

**MATH 445. Nonlinear Dynamics and Chaos Theory. 3 Hours.**

The study of differential equations from a geometric perspective that allows for exploration of two and three-dimensional systems. Topics will include linear systems of equations, linear stability analysis, and bifurcations of nonlinear systems, and chaos theory.

**Prerequisite:** MATH 220 with a minimum grade of D and MATH 240 with a minimum grade of D.

**MATH 446. Partial Differential Equations. 3 Hours.**

A detailed introduction to partial differential equations. Students will develop familiarity with the derivation and solution techniques for various equations including transport equations, the heat equation, wave equation, and Laplace equation.

**Prerequisite:** (MATH 210 with a minimum grade of D or MATH 212 with a minimum grade of D) and MATH 240 with a minimum grade of D.

**MATH 448. Functions of a Complex Variable. 3 Hours.**

An introduction to the analysis of functions of a complex variable. Topics will include differentiation, contour integration, power series, Laurent series, and applications.

**Prerequisite:** MATH 260 with a minimum grade of D.

**MATH 470. Independent Study in Math. 1 to 3 Hours.**

Independent study of selected topics in Mathematics at an advanced level. Specific topics vary from semester to semester.

**MATH 480. Advanced Topics in Mathematics. 1 to 4 Hours.**

Advanced topics in undergraduate mathematics offered occasionally to meet special needs. Typical topics include number theory, foundations of mathematics, topology, and complex variables.

**MATH 500. Honors Course. 3 Hours.**

At the discretion of the faculty, students may undertake a six-hour independent course of study in the senior year in order to broaden their educational experience within their major area of study. Students must meet specific GPA standards and arrange a faculty sponsor. The honors course criteria are outlined in the Academic Honors portion of the catalog.